

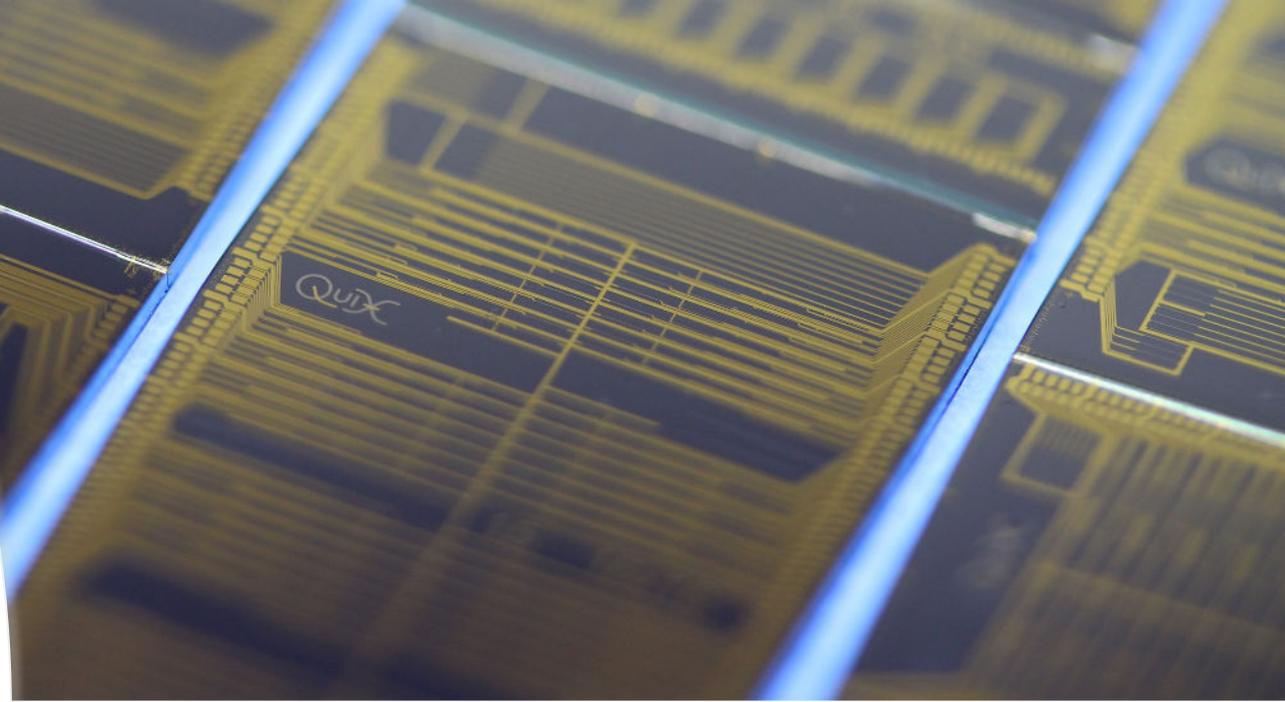
Integrated photonic quantum information processing

Jelmer Renema
University of Twente
j.j.renema@utwente.nl



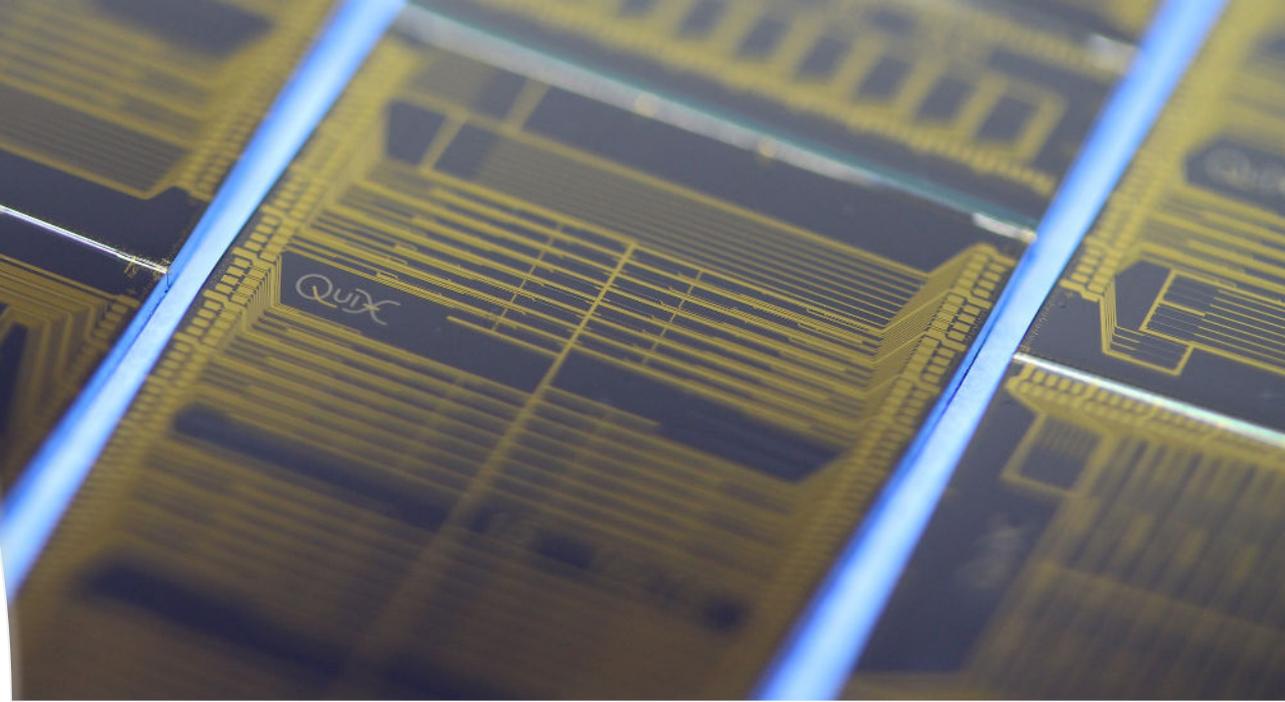
Photonics leads quantum

- Room-temperature operation
- High compatibility with telecom
- Intrinsic datacenter compatibility



Photonic quantum computing in NL

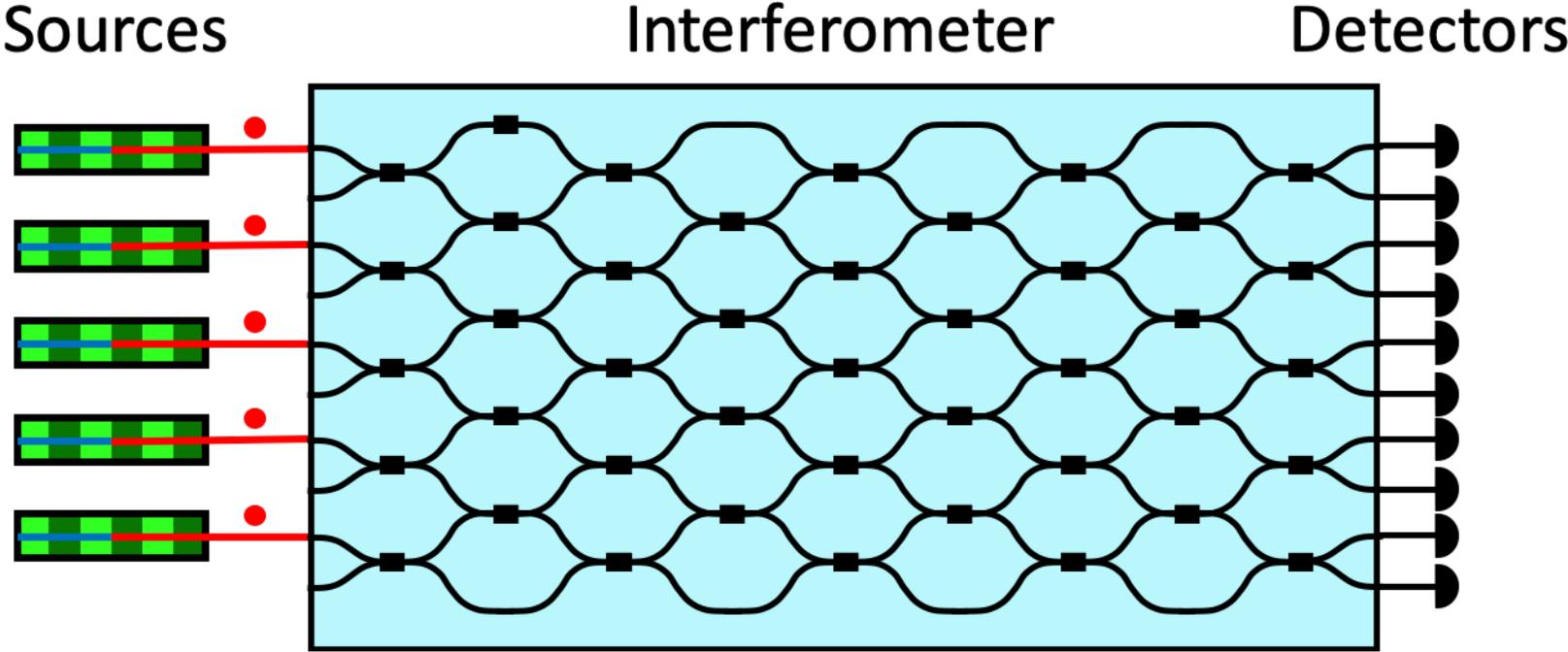
- First sale of quantum hardware in NL
- First sale of quantum computer in NL
- Only system integrator in the quantum space
- Quantum advantage demonstration
- Today: academic efforts on quantum photonics @ U Twente



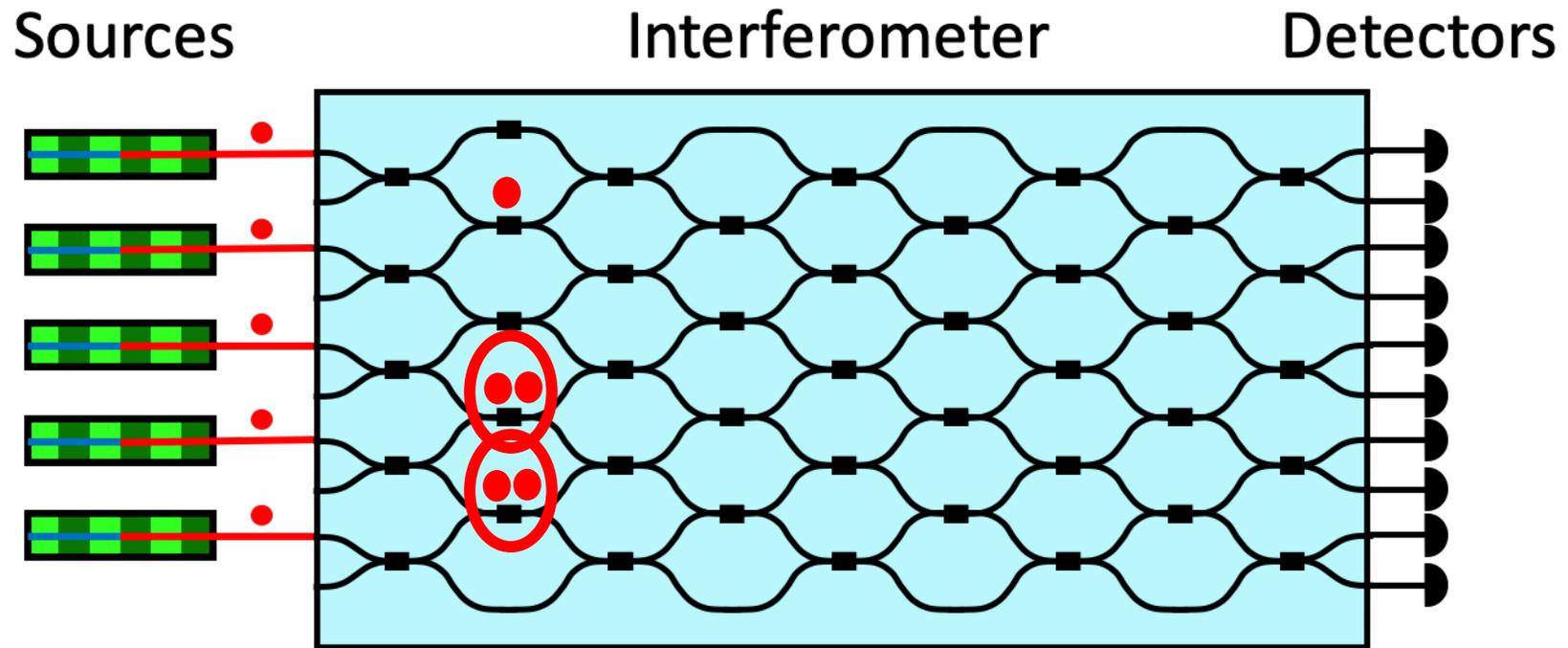
The team



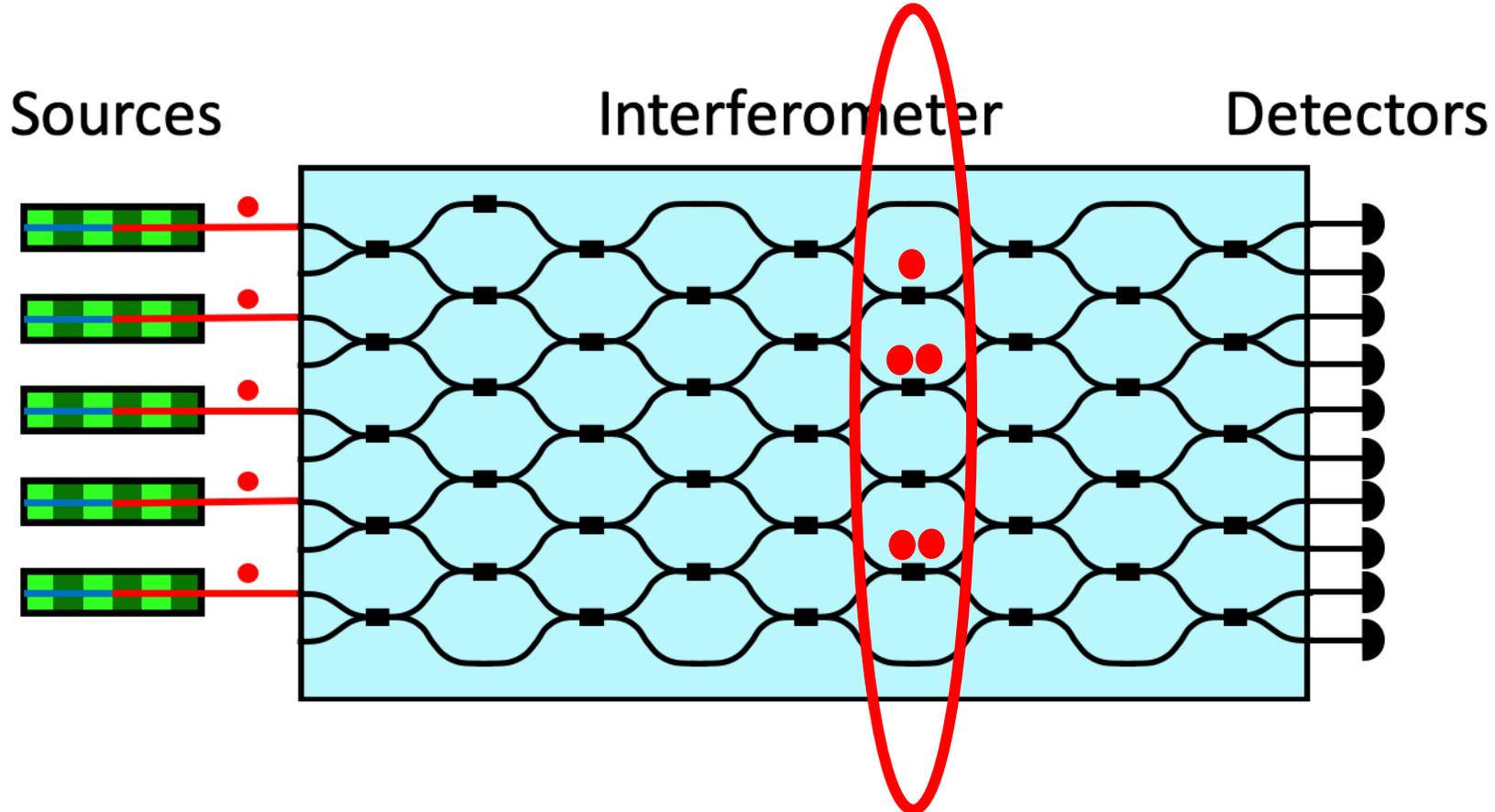
The system



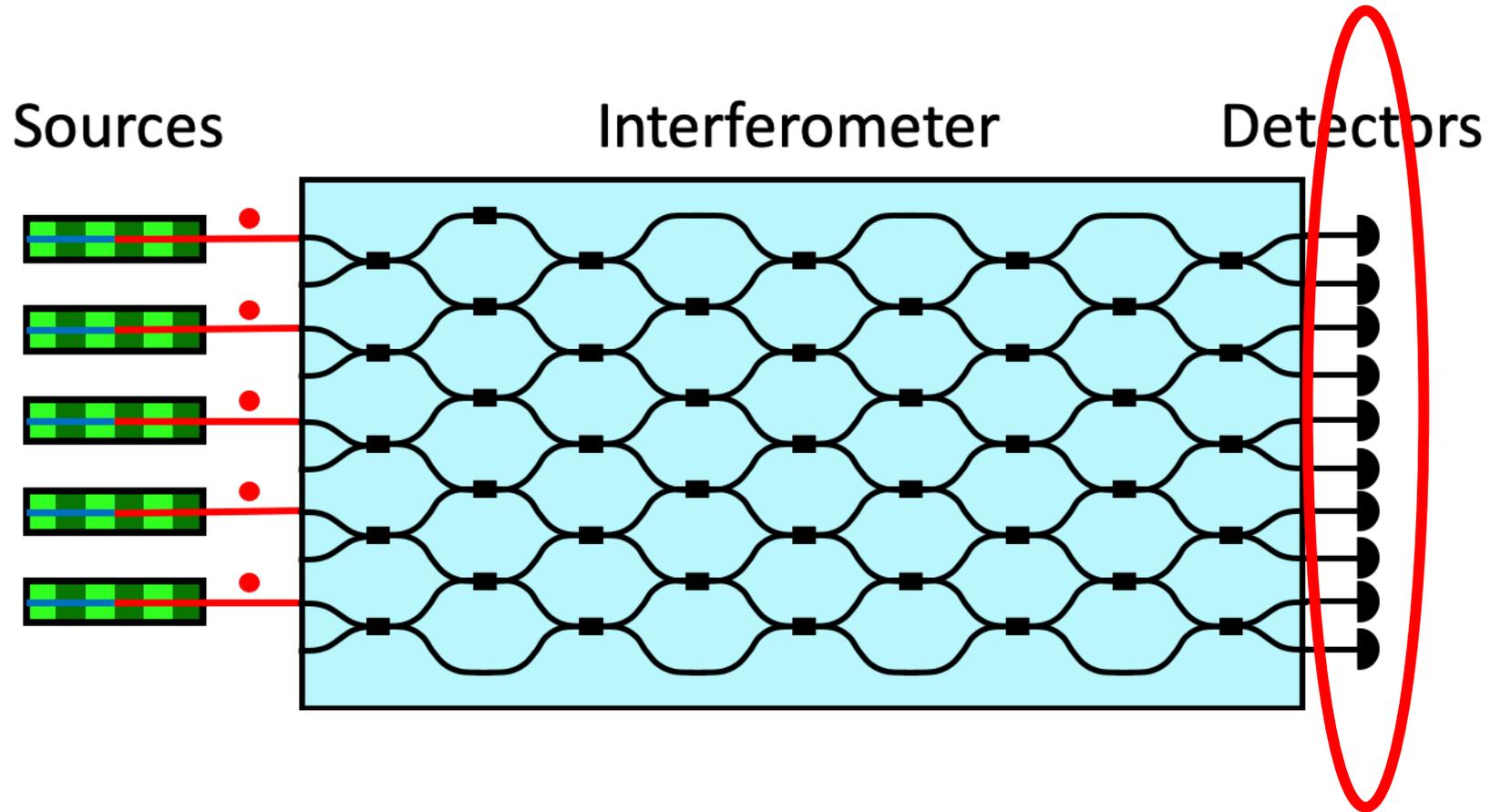
The system



The system

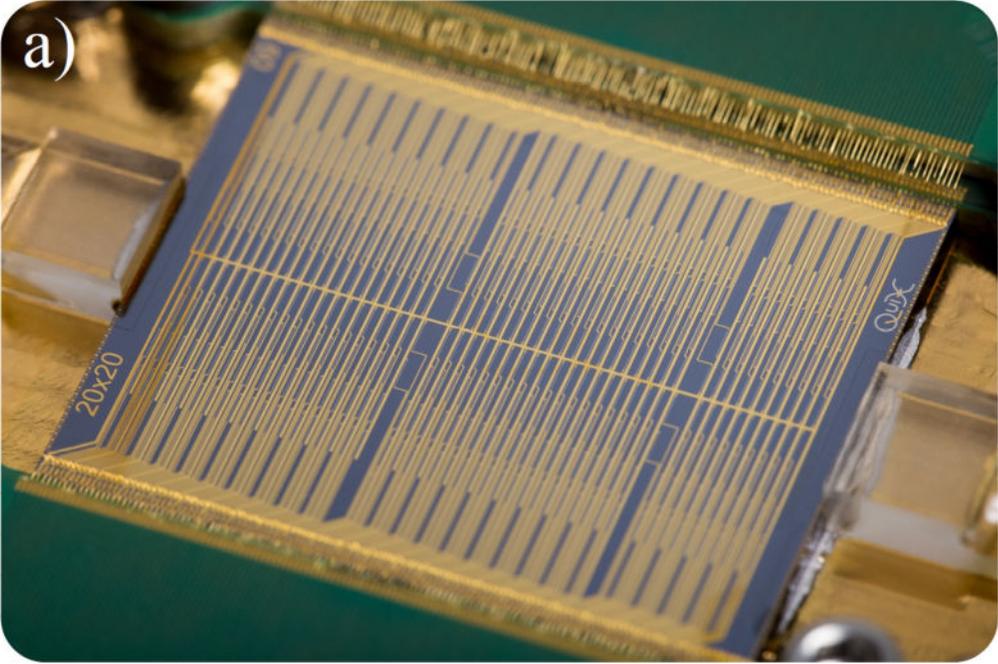
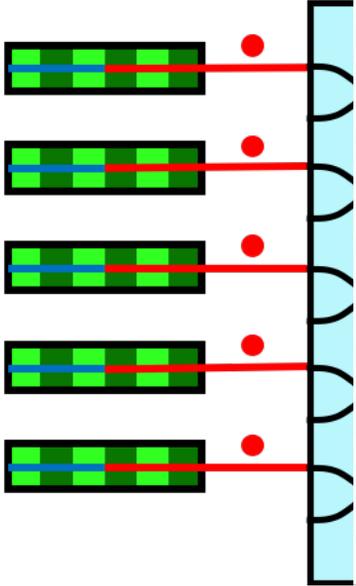


The system



The system

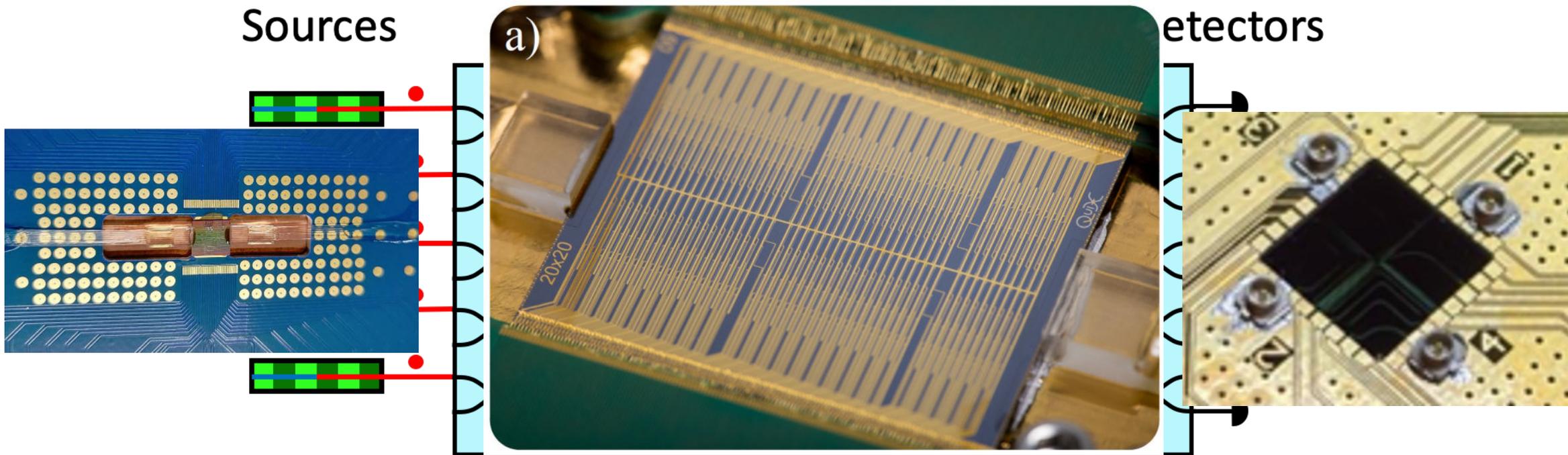
Sources



Detectors



The system



Near-term quantum computation: Monte-Carlo integrator



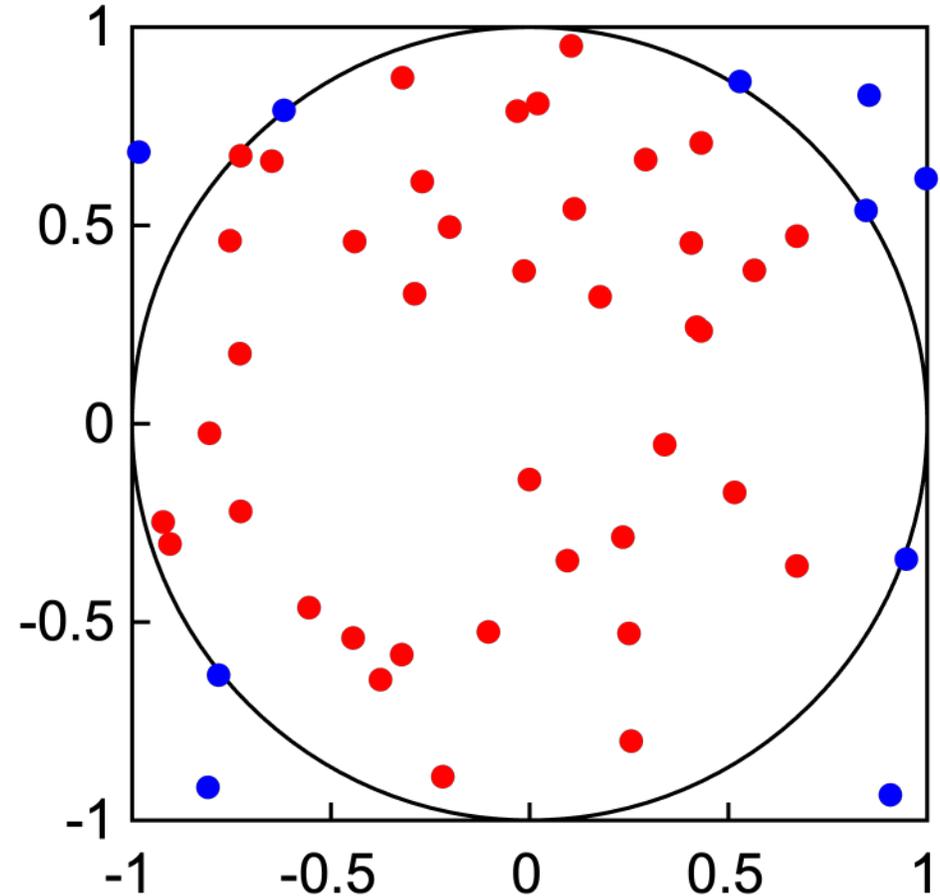
Finding useful applications for NISQ

- Many, many, false starts in finding applications for NISQ
- Big problem: NISQ only has quantum advantage for the task of drawing samples!
- Need to find situations where quantum-weighted lotteries are useful



Monte carlo integration

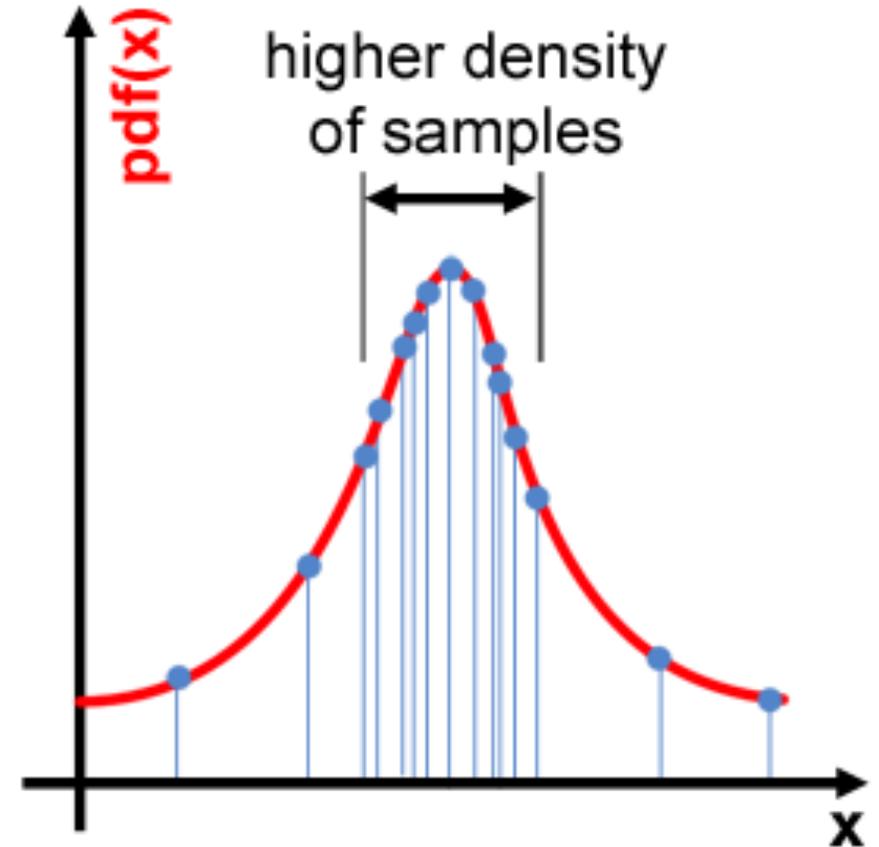
- Compute π by uniformly throwing darts at a dart board
- $\frac{A_{circ}}{A_{sq}} = \frac{\#in}{N}$
- Error guaranteed to go as $\epsilon \propto C \frac{1}{\sqrt{N}}$
- With C given by 'how much your distribution resembles your function'



Monte carlo integration

- Compute π by uniformly throwing darts at a dart board
- $\frac{A_{circ}}{A_{sq}} = \frac{\#in}{N}$
- Error guaranteed to go as $\epsilon \propto C \frac{1}{\sqrt{N}}$
- With C given by 'how much your distribution resembles your function'

© www.scratchapixel.com



The one bit of mathematics – importance sampling

Suppose we want to integrate a function of the form

$$f(x) = g(x)h(x)$$

$$\text{Then } \int f(x)dx = \int g(x)h(x)$$

$$= \int_{g(x)} h(x)dg(x)$$

$$\approx \frac{1}{N} \sum_{g(x)} h(x)$$

The one bit of mathematics – importance sampling

Suppose we want to integrate a function of the form

$$f(x) = g(x)h(x)$$

$$\text{Then } \int f(x)dx = \int g(x)h(x)$$

$$= \int_{g(x)} h(x)dg(x)$$

$$\approx \frac{1}{N} \sum_{g(x)} h(x)$$

Now suppose $g(x)$ happens to be implementable on quantum hardware...

The one bit of mathematics – importance sampling

Suppose we want to integrate a function of the form

$$f(x) = g(x)h(x)$$

$$\text{Then } \int f(x)dx = \int g(x)h(x)$$

$$= \int_{g(x)} h(x)dg(x)$$

$$\approx \frac{1}{N} \sum_{g(x)} h(x)$$



$g(x)$ -weighted lottery!

Now suppose $g(x)$ happens to be implementable on quantum hardware...

The one bit of mathematics – importance sampling

Suppose we want to integrate a function of the form

$$f(x) = g(x)h(x)$$

Then $\int f$ Do such cases arise in practice?

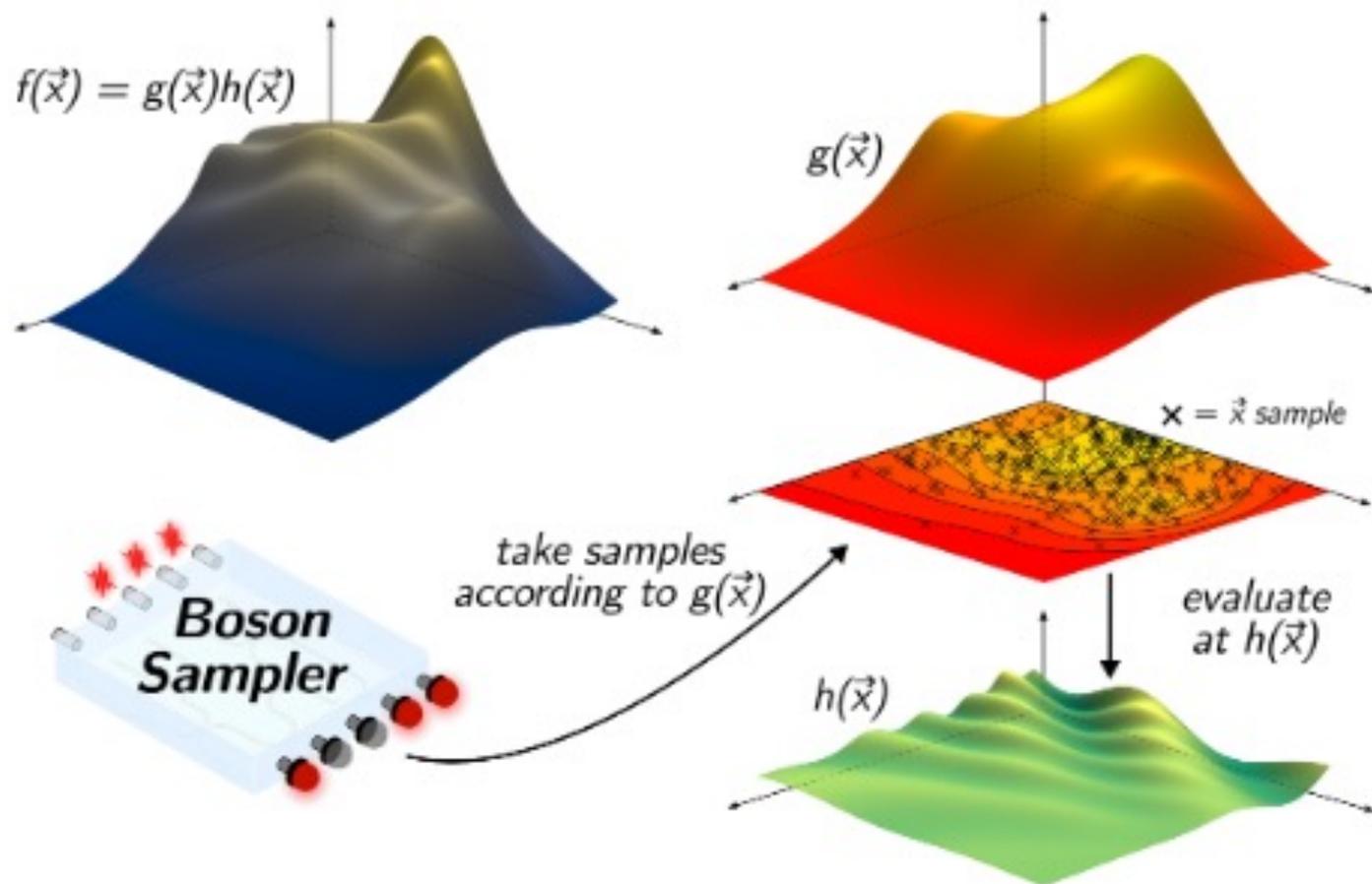
$$= \int_{g(x)} h(x) dg(x)$$

$$\approx \frac{1}{N} \sum_{g(x)} h(x)$$



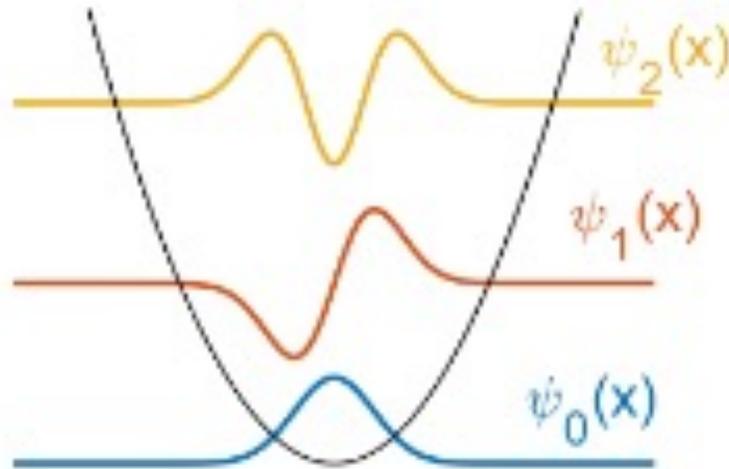
$g(x)$ -weighted lottery!

Now suppose $g(x)$ happens to be implementable on quantum hardware...



Yes: first-order perturbation theory

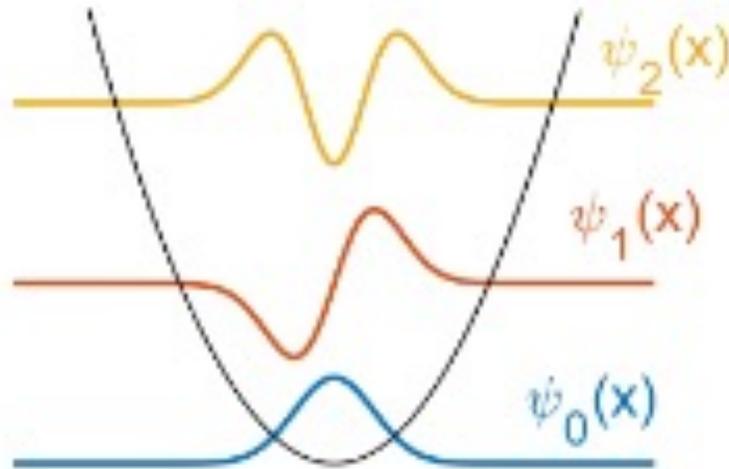
$$E_1 = \langle \psi(x) | V(x) | \psi(x) \rangle = \int dx V(x) |\psi(x)|^2$$



Yes: first-order perturbation theory

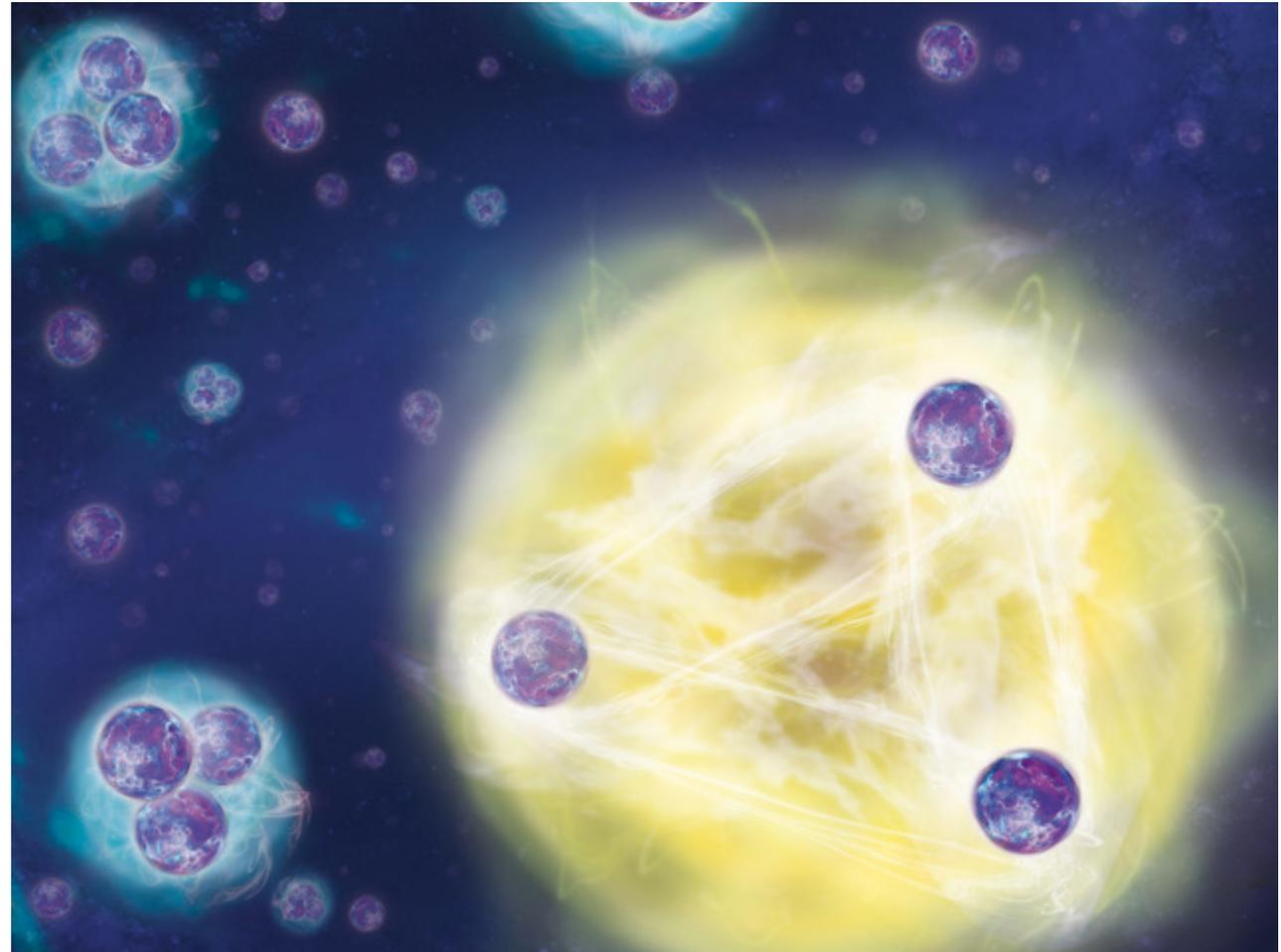
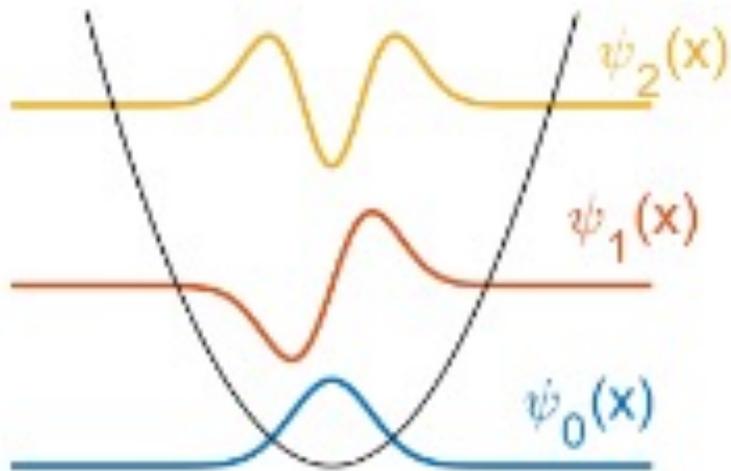
$$E_1 = \langle \psi(x) | V(x) | \psi(x) \rangle = \int dx V(x) |\psi(x)|^2$$

Do such cases arise in practice?



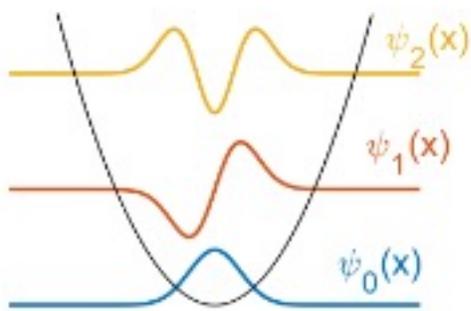
Yes: Efimov physics

$$V_{\text{Ef}}(\vec{x}) = -\frac{C + 1/4}{R^2}$$

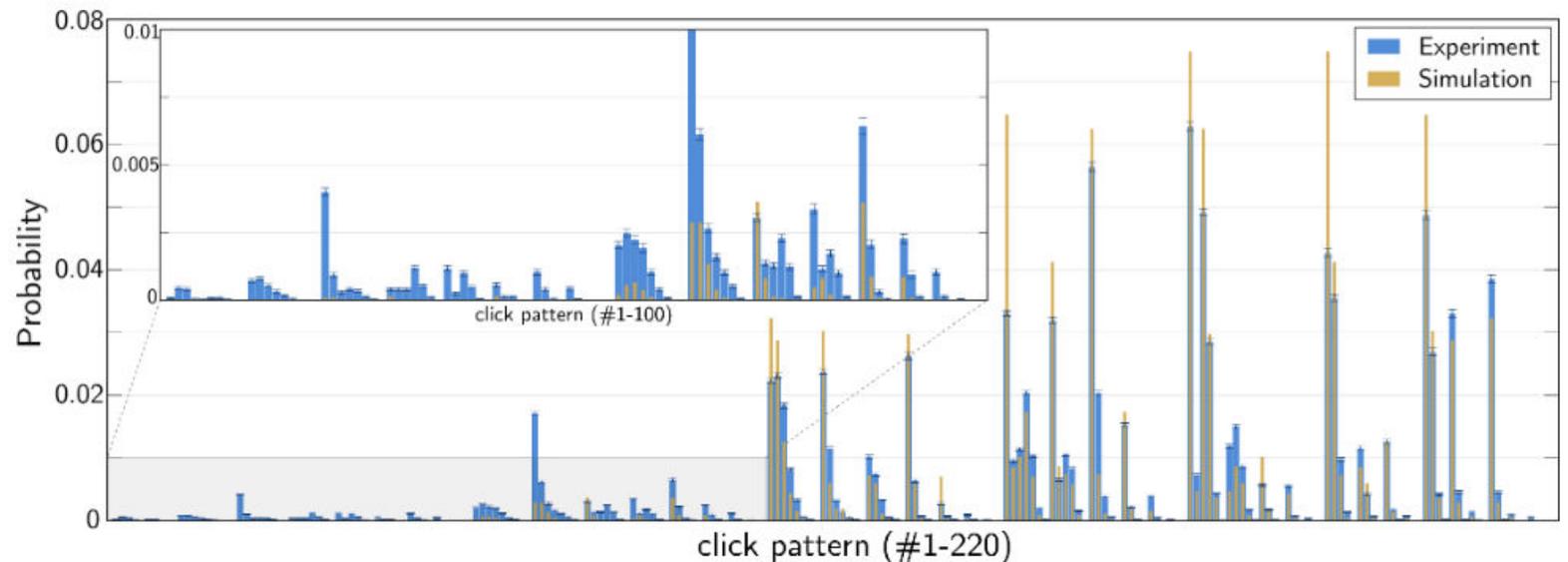


Quantum-assisted Monte-Carlo integrator

Efimov potential in a harmonic trap – lowest three states

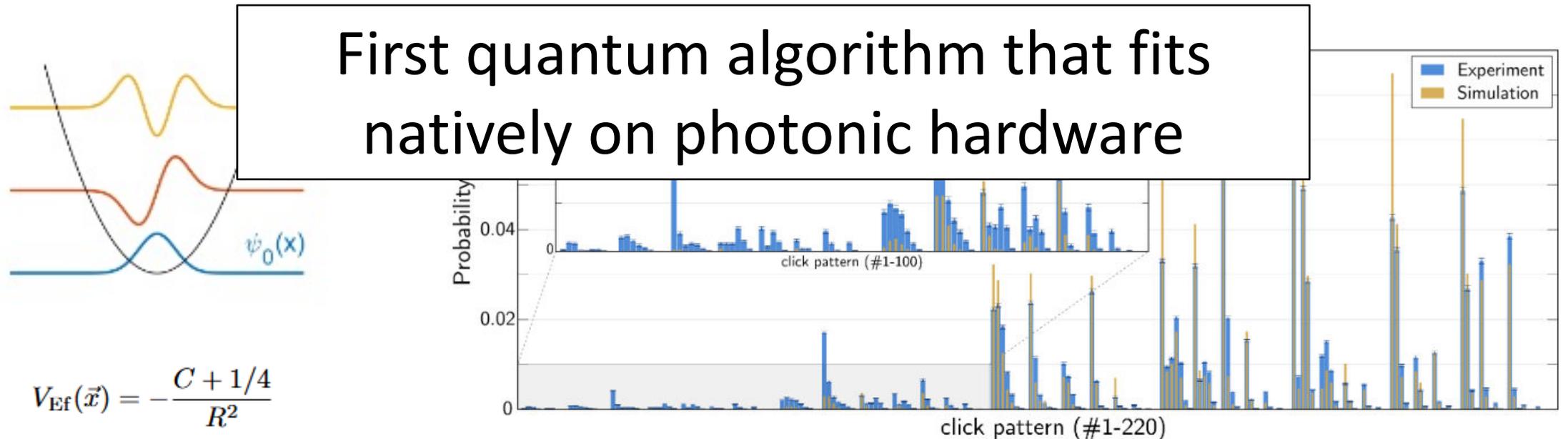


$$V_{\text{Ef}}(\vec{x}) = -\frac{C + 1/4}{R^2}$$

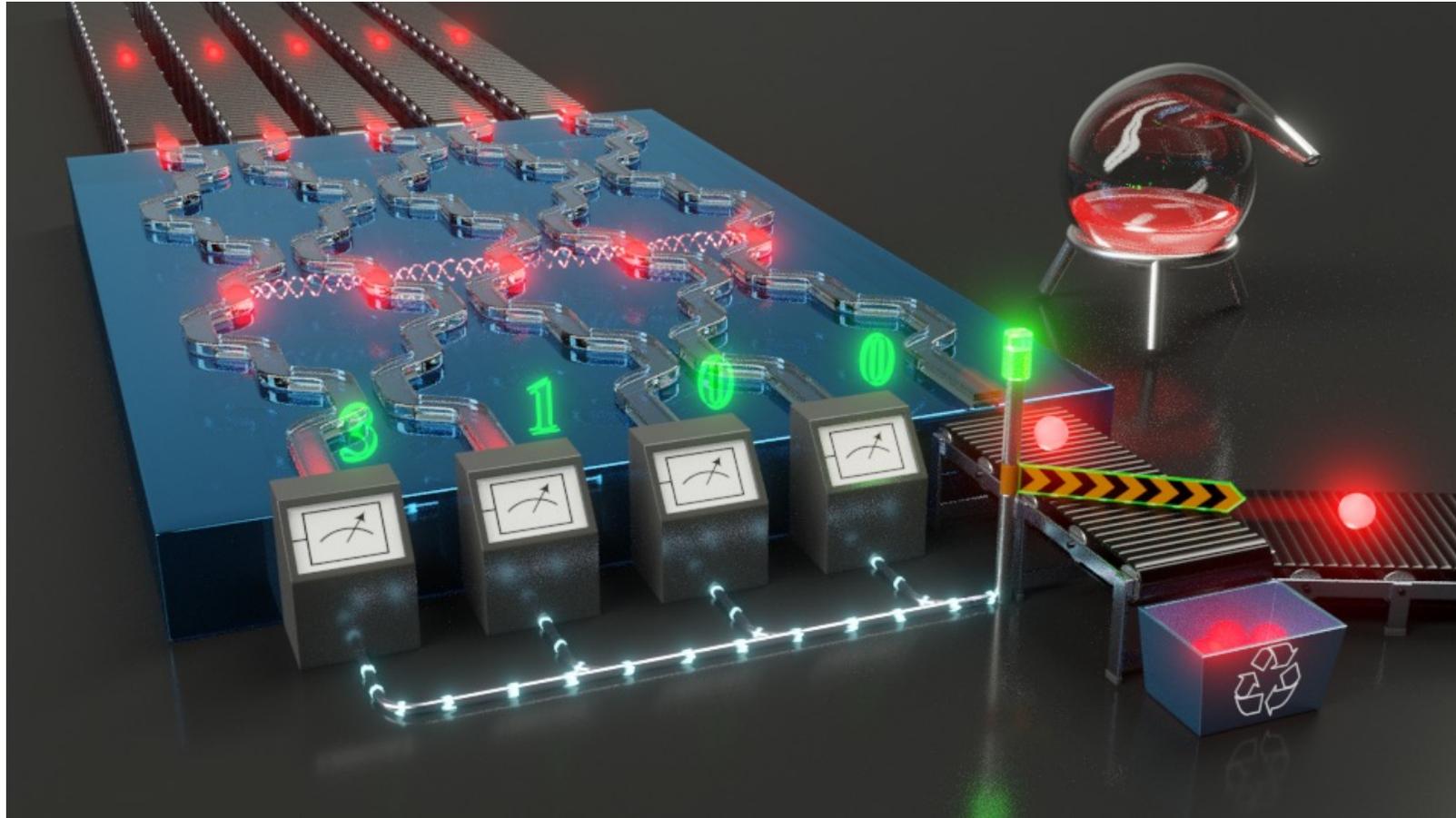


Quantum-assisted Monte-Carlo integrator

Efimov potential in a harmonic trap – lowest three states



Universal quantum computation: Photon distillation



Suppose you want to build a photonic QC

You need lots and lots of single photons

So, lots and lots of shots from a single photon source

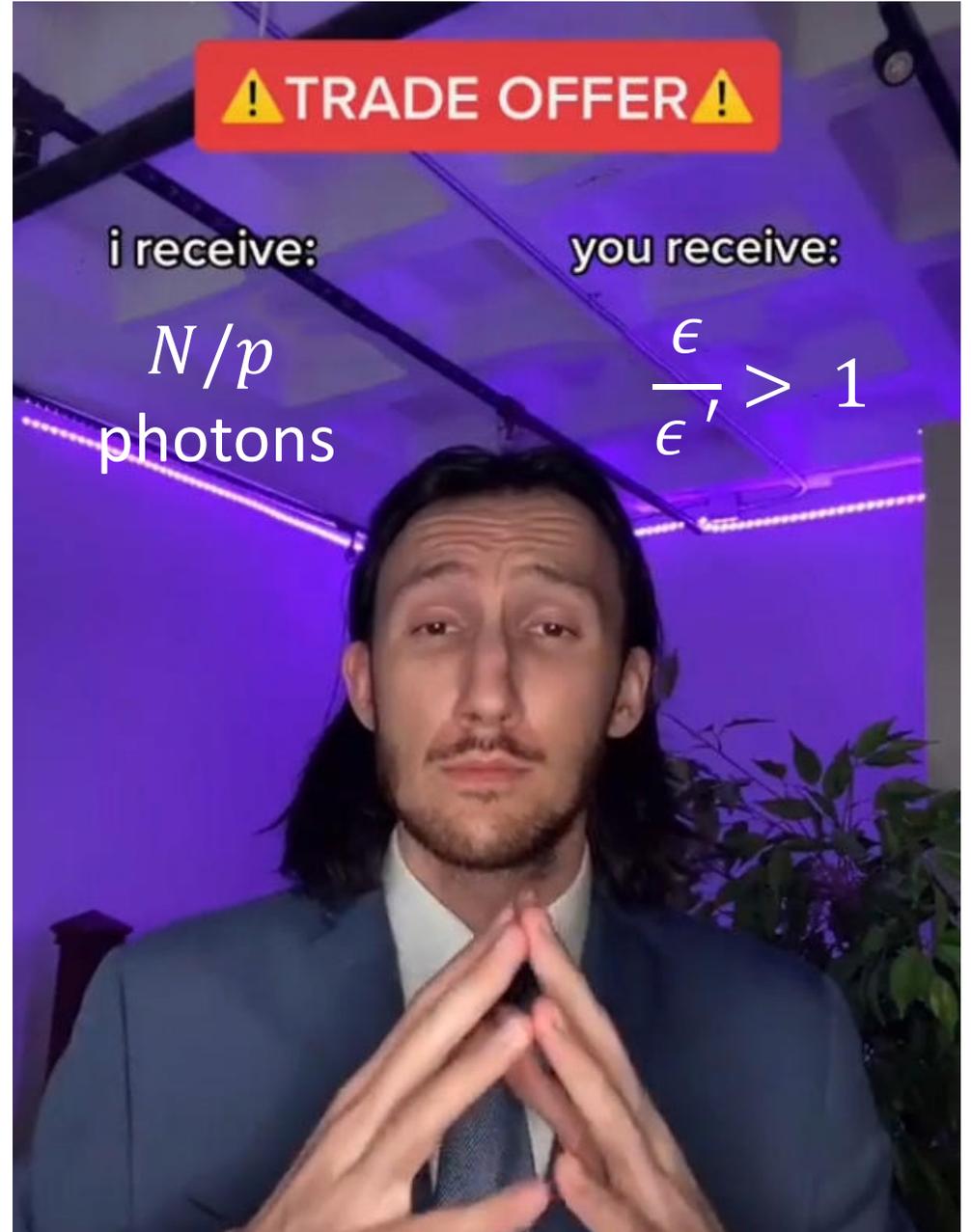
OOM estimate: 10^6 qubits,
 10^1 photons per qubit,
 10^2 multiplexing per photon

Regime where tuning up a single source doesn't make sense anymore



Photon distillation

Probabilistically trade N “bad” photons with error ϵ for *one* “better” photon $\epsilon' < \epsilon$ with probability p .



Setting up the problem

Orthogonal bad bit model

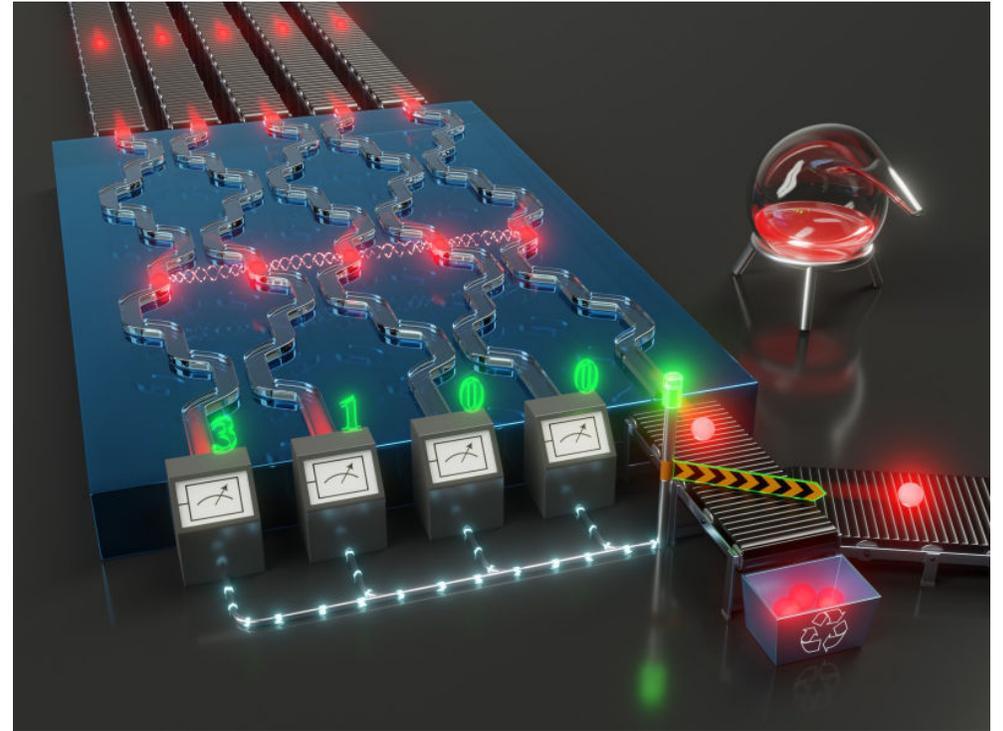
- Indistinguishable $P(\bullet) = (1 - \epsilon)$
- Distinguishable $P(\blacklozenge) = \epsilon$
- $\rho_T = \rho^{\otimes N}$ with $\rho = (1 - \epsilon)|1_g\rangle\langle 1_g| + \epsilon|1\rangle_b\langle 1|_b$
- Circuit U
- Compute $\rho_{out}(M)$ using standard techniques

Photon distillation

How to decrease ϵ ?

→ Find  and U such that

$$\frac{P(\bullet | \text{eye})}{P(\bullet)} > 1$$



Photon distillation

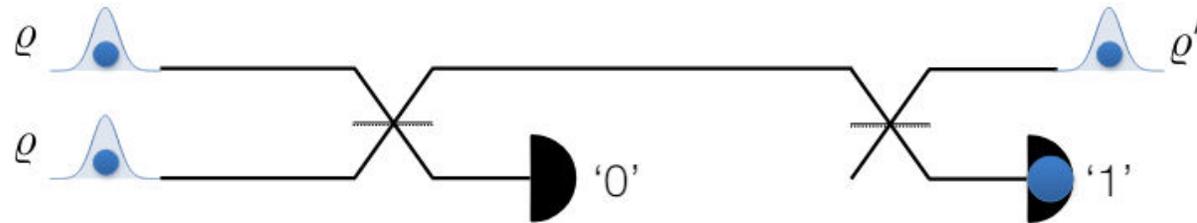
How to decrease ϵ ?

→ Find  such that

How to decrease ϵ ?
→ Find such  
First proposal: 10^{1049} photons for $\frac{\epsilon'}{\epsilon} = 100$, by concatenation

First proposal: 10^{1049} photons for $\frac{\epsilon'}{\epsilon} = 100$, by concatenation

$$\epsilon' = \frac{\epsilon}{N}$$



Photon distillation

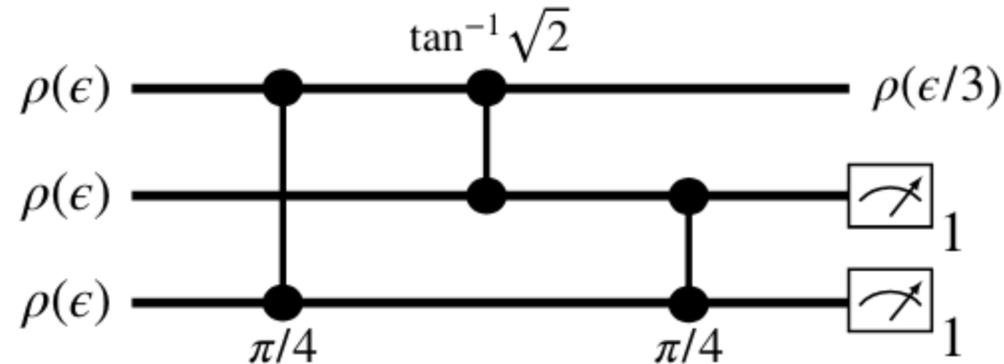
How to decrease ϵ ?

→ Find  such that $\frac{P(\bullet | \text{eye})}{P(\bullet)} > 1$

Second proposal: 59000 photons for $\frac{\epsilon'}{\epsilon} = 100$, by concatenation

$$\epsilon' = \frac{\epsilon}{3}$$

$$p = \frac{1}{3}$$



Photon distillation

How to decrease ϵ ?

→ Find  such that

$$\frac{P(\bullet | \text{eye})}{P(\bullet)} > 1$$

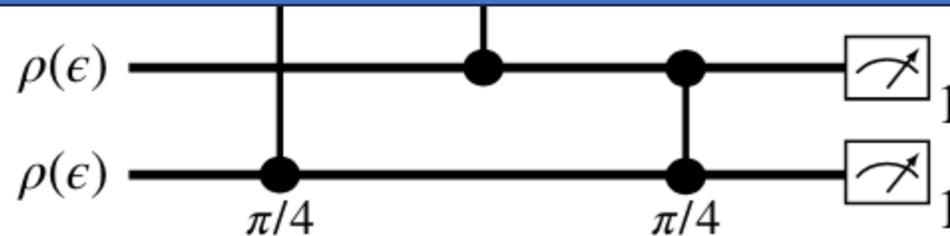
Second p

tion

$$\epsilon' = \frac{\epsilon}{3}$$

$$p = \frac{1}{3}$$

Can we do better?



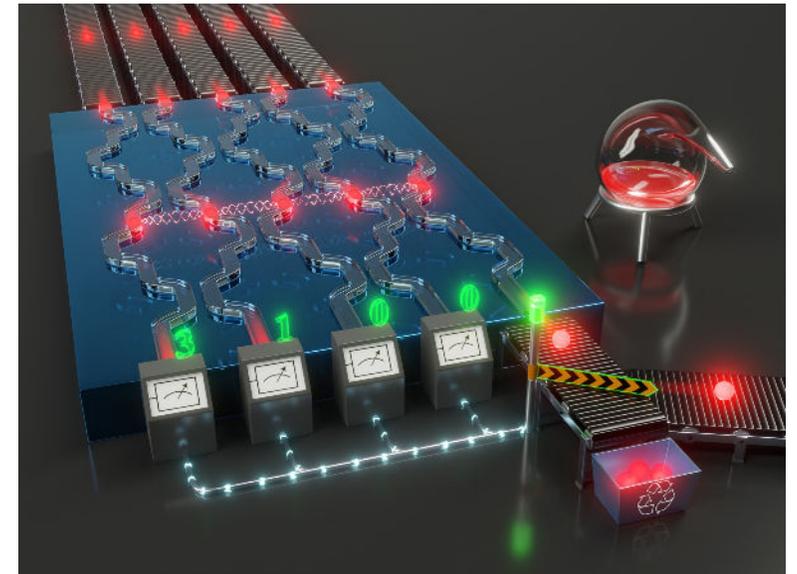
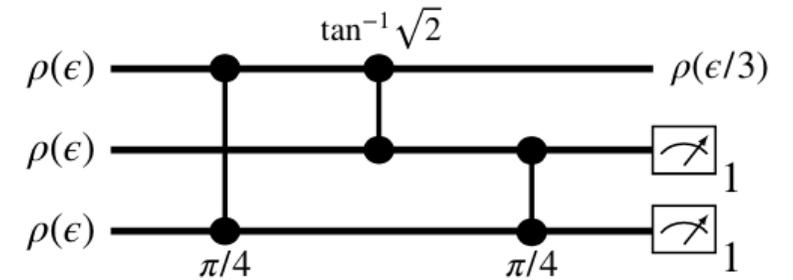
Realization

Scheme of [1] = 3-mode Fourier transform!

That gives a way to generalize: N photons in N modes

$$\rightarrow \epsilon' = \frac{\epsilon}{N}?$$

$$\rightarrow p = \frac{1}{N}?$$



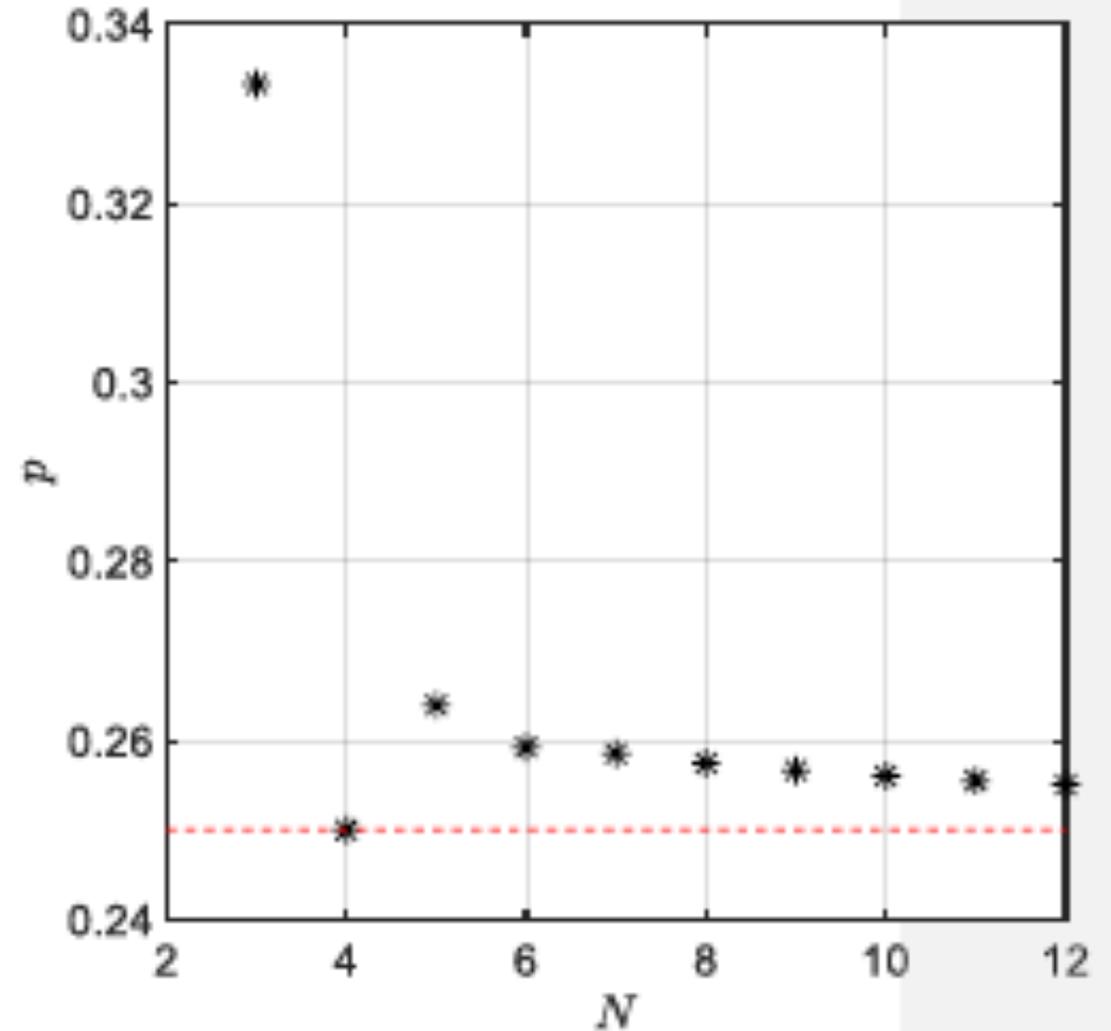
N-photon distillation

Simulations on N -mode
Fourier transform

$$p = \sum_{j=0}^N (-1)^j (j+1) \prod_{i=1}^j \left(1 - \frac{i}{N}\right)$$

$p \rightarrow \frac{1}{4}$ (proof by NASA Ames)

$$\epsilon' = \epsilon/N$$



N-photon distillation

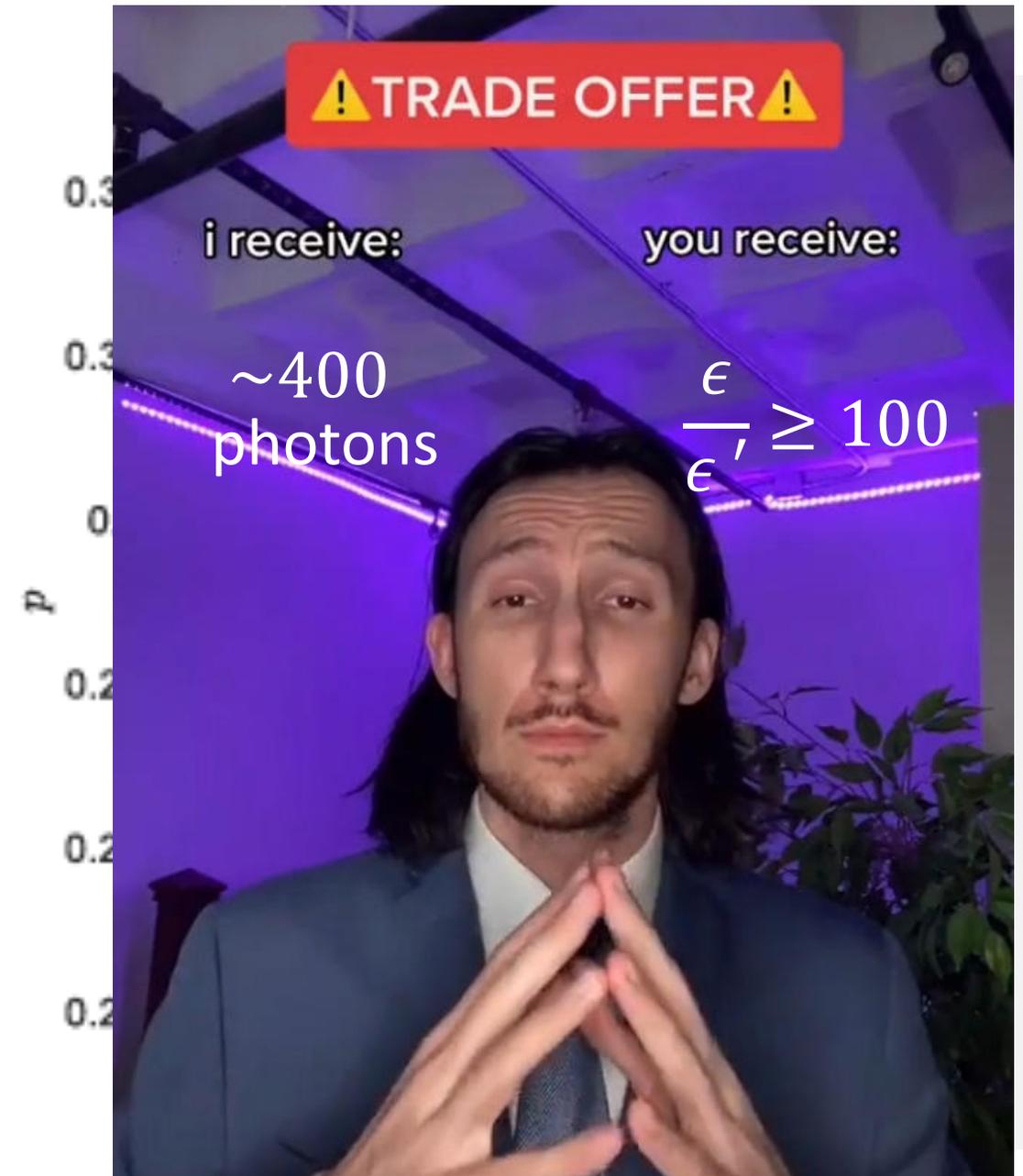
Simulations on N -mode
Fourier transform

$$p = \sum_{j=0}^N (-1)^j (j+1) \prod_{i=1}^j \left(1 - \frac{i}{N}\right)$$

$$p \rightarrow \frac{1}{4} \text{ (proof by NASA Ames)}$$

$$\epsilon' = \epsilon/N$$

No concatenation required!!

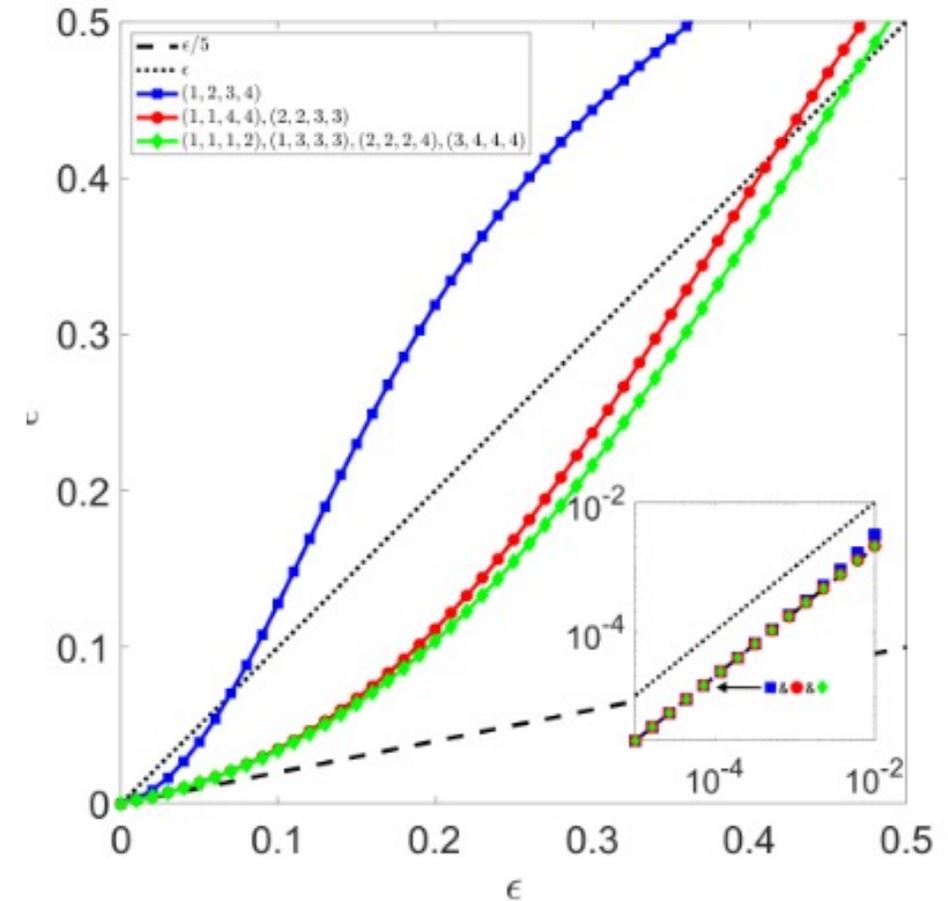


Photon distillation vs error correction

- Photon distillation has a higher threshold for photon distinguishability than error correction w/ surface code
- Photon distillation + error correction is a more efficient use of resources (as measured in photon sources) than just error correction

Behaviour above threshold

- For the surface code: error threshold is about 0.6% to 1%
- For photon distillation: error threshold is at least 10%, probably more
- Moreover, there's also photon loss!



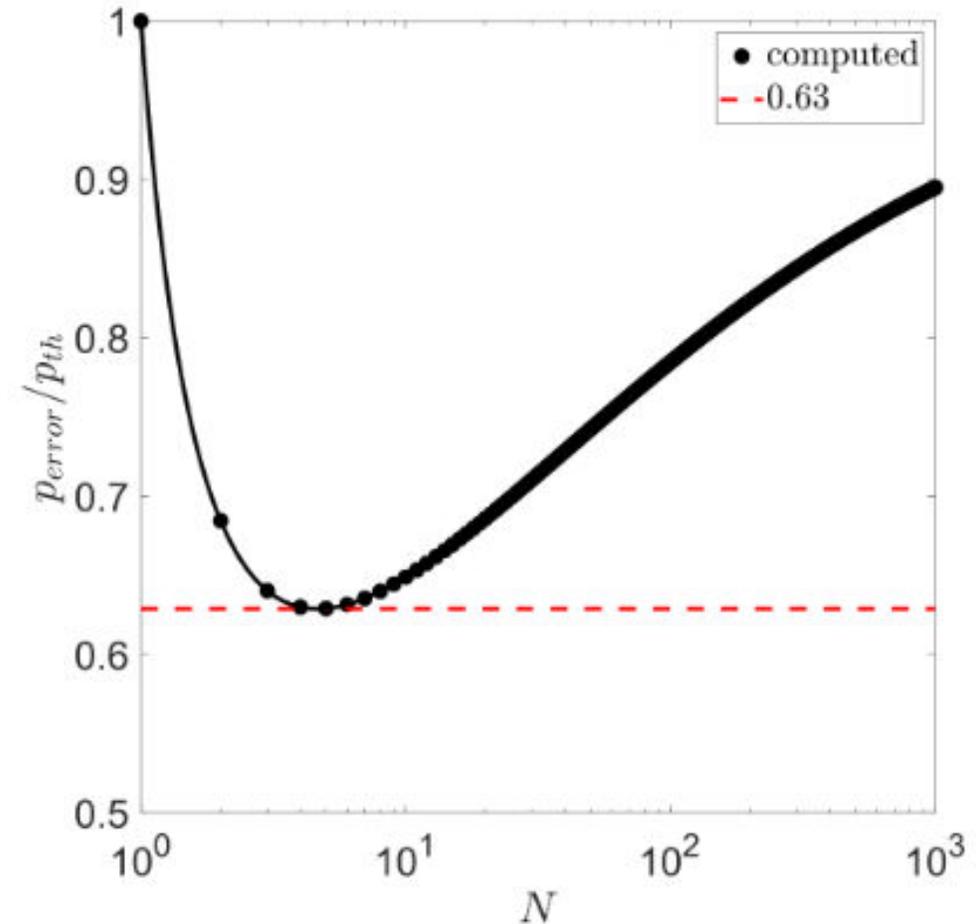
Behaviour below threshold

- Assume linear interchange between Pauli errors and photon errors

$$p_{error} = \alpha \epsilon$$

$$C_L^{dist.} = C_L \cdot \left(\frac{2\sqrt{N} \log\left(\frac{p_{error}}{p_{th}}\right)}{\log\left(\frac{p_{error}}{p_{th}}\right) - \log(N)} \right)^2.$$

- Also turns out: nonlinear relation helps us



Conclusion

- Indistinguishability errors can be reduced by photon distillation.
- Lowest resource costs scaling to date:
 $\epsilon' = \frac{\epsilon}{N}$ requires $\sim 4N$ photons.
- This component will turn up in real photonic quantum computers!

